

In-class Activity 2

Limits

LAST NAME: _____ FIRST NAME: _____

Question 1 Compute the following limits:

$$(1) \lim_{t \rightarrow 0} \frac{\sin(10t)}{t} =$$

$$(2) \lim_{h \rightarrow 0} \frac{2h}{\sin(5h)} =$$

$$(3) \lim_{x \rightarrow 0} \frac{x^2}{\sin(x)} =$$

Question 2 Compute the following limits, specifying if they result in $-\infty$ or $+\infty$:

$$(1) \lim_{x \rightarrow 2^-} \frac{4}{x-2} =$$

$$(2) \lim_{u \rightarrow 3^+} \frac{u-1}{3-u} =$$

$$(3) \lim_{x \rightarrow 0^+} \frac{\cos(x)}{x} =$$

Question 3 Compute the following limits. Interpret your answer geometrically in terms of asymptotes.

$$(1) \lim_{x \rightarrow -\infty} \frac{3x^4 - x^5}{x + x^5} =$$

$$(2) \lim_{t \rightarrow -\infty} \frac{2t}{t^2 - 1} =$$

$$(3) \lim_{x \rightarrow \infty} \frac{x^{10}}{x^2 - 3x^5} =$$

Question 4 Compute the following limits, if they exist, or write “Does not exist” and justify why. Quote any Theorems or Results you are using:

$$(1) \lim_{x \rightarrow 0} x^6 \sin\left(\frac{6}{x}\right) =$$

$$(2) \lim_{x \rightarrow \infty} \frac{\cos(x)}{x} =$$

$$(3) \lim_{x \rightarrow 0} \frac{2}{x} \sin(6x) =$$

Question 5 Find all horizontal and vertical asymptotes for the function

$$f(x) = \frac{x^2 - 2x + 1}{x^2 - 1}$$

Question 6 Give an example of a function f that has asymptotes $x = 0$, $y = 1$ and such that $f(0) = 5$.

Question * Compute the following limits if they exist, or write “Does not exist” and justify why:

$$(1) \lim_{x \rightarrow 2} \frac{|x - 2|}{x - 2} =$$

$$(2) \lim_{u \rightarrow -3} \frac{u^2 + 6u + 9}{|u + 3|} =$$

$$(3) \lim_{x \rightarrow 0} \frac{|x| - x}{2x} =$$